

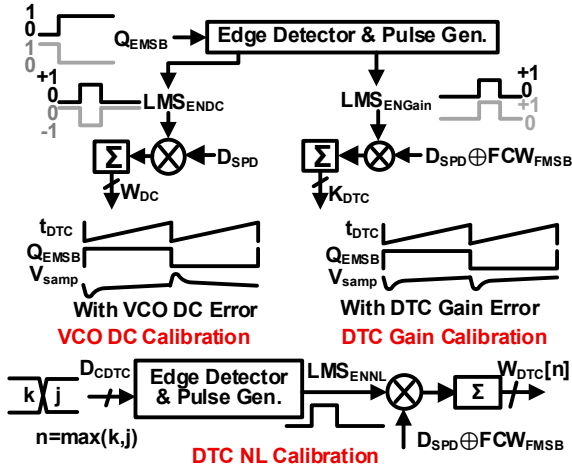


Fig. 2. Block diagram of the gated-LMS-based VCO DCC, DTC gain nonlinearity calibration

gated-LMS VCO DCC uses an edge detector to detect the transitions of Q_{EMSB} and a pulse generator to generate a signed LMS enable signal (LMS_{ENDC}). This signal is correlated with D_{SPD} and accumulated to tune W_{DC} . Similarly, with DTC gain error and the dual edge retimer, the V_{smp} also generates narrow pulses with the same polarity at both Q_{EMSB} transition edges rather than only after the division ratio pulse [2,3]. The DTC gain error and NL-induced narrow pulses polarities change with different FCW_{FMSB} , where FCW_{FMSB} is the MSB of the fractional frequency control word (FCW). Two unsigned LMS enable signals LMS_{ENGain} and LMS_{ENNL} are thus generated, correlated with $D_{SPD} \oplus FCW_{FMSB}$ and then accumulated to update K_{DTC} and $W_{DTC}[15:1]$ for gain and NL calibration respectively. At the medium-integer and far-integer settings, the SPD output pulse may overlap with subsequent pulses and affect the stability of gated-LMS calibration. Fortunately, since the error signals at SPD output are not filtered out by the PLL loop, conventional LMS calibration can be applied to DTC gain and nonlinearity and VCO duty-cycle calibration.

C. Circuit Implementation

The merged DTC-SPD performs quantization error cancellation in SPD without DTC by using either a resistive DAC (RDAC) [6,7], CDAC [11,12] or a switched capacitor (SC) approach [10]. The RDAC consumes static power and slows down settling time, while existing CDAC-based DTC-SPD designs require a transmission gate (TG) as sampling switch between the sampling capacitor and the switched current source. The TG exhibits large ON-resistance when the sampled voltage is close to half of the supply voltage, which limits the rise time of the voltage across the sampling capacitor and thus limits available detection gain. The SC-based DTC-SPD have strong NL caused by switch resistance [10], which becomes worse with a higher detection gain. Although NL can be compensated by using charge injection [10], the compensation accuracy is vulnerable to PVT variations, which is similar to digital predistortion without calibration. Therefore, a merged DTC-SPD with CDAC without a TG-based sampling switch is used as shown in Fig.3. The charging current is turned on when both CK_{BUF} and CK_{DIV} are low. As part of the charging capacitance, the CDAC adds only minimal extra dynamic power consumption. After compensation, a comparator is triggered to convert the

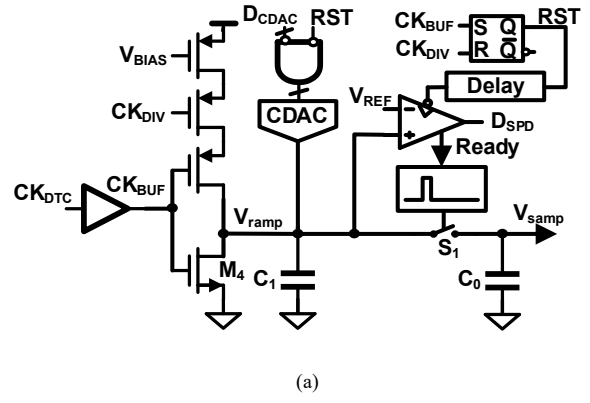


Fig. 3. (a) Schematic of the merged DTC-SPD with CDAC (b) timing diagram of DTC-SPD

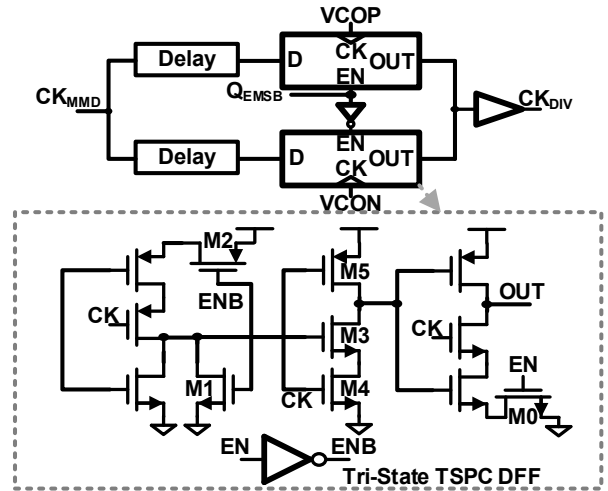


Fig. 4. Schematic of the dual-edge retimer with tri-state TSPC DFFs

phase error polarity into a 1-bit output (D_{SPD}) for calibration and the integral path. The compensated sampled voltage is transferred to the output holding capacitor (C_0) to control the proportional-path varactor after comparison to avoid pulse amplitude reduction [3]. The simulated input-referred integral NL is within 44fs with a detection gain of 15.8GV/s.

Fig.4 shows the dual-edge retimer employing tri-state TSPC DFFs. Conventionally, a dual-edge retimer is realized using two cascaded DFFs with an output MUX [4,7], which requires two high-speed DFFs operating simultaneously, thereby doubling power consumption. Therefore, the proposed design utilizes two tri-state TSPC DFFs operating complementarily with a shared output, reducing power

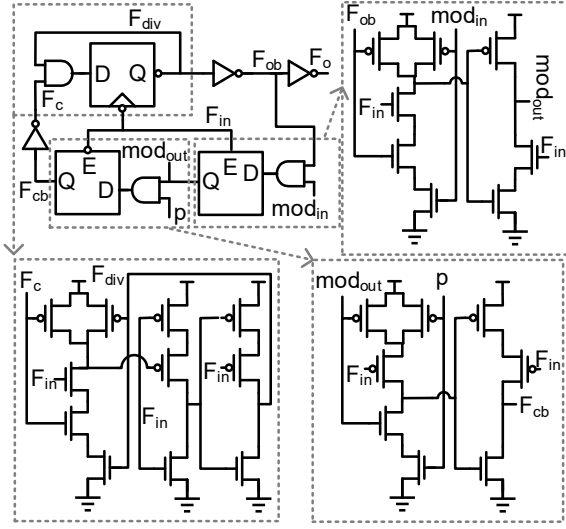


Fig. 5. Schematic of divided-by 2/3 frequency prescaler

consumption. In the off state of TSPC DFF, M3 is disabled to prevent high-speed dynamic current through M4 and M5, while M0 is turned off to leave the output stage in a high-impedance state, allowing it to be shared with the other DFF. To meet setup and hold-time requirements, two different delay lines are inserted between CLK_{MMD} and the DFF inputs.

The MMD is implemented by cascading divided-by 2/3 cells [8]. Since the MMD output is retimed to remove output jitter, it uses a transistor width of 90nm for the first two stages to save power. To maintain high speed operation with small size, the first two stages use TSPC-based DFF and latches with merged AND gate as shown in Fig.5 and the first stage uses ultra-low-threshold-voltage transistors.

III. MEASUREMENT RESULTS

The presented fractional-N PLL occupies a core area of 0.11mm^2 , as shown in Fig.9 and TABLE I. It consumes only 0.88mW (TABLE I) with a 100MHz reference input and $FCW=64+2^{-14}$. Fig.6 and Fig.7 show the measured output phase noise spectrum in integer-N and fractional-N mode. Fig.8 shows the measured output jitter and fractional spur levels with different fractional FCW (FCW_F). When approaching far-integer settings, the V_{samp} output pulses overlap with subsequent pulses, destabilizing the gated-LMS calibration. For $FCW_F < 2^{-6}$, gated-LMS calibration is applied to DTC gain, NL, and VCO DC. For $FCW_F \geq 2^{-6}$, the DTC NL calibration is then switched to conventional LMS calibration algorithm, and for $FCW_F \geq 2^{-4}$, both the DTC gain and VCO DC calibrations are changed to LMS mode for stable calibration. The worst-case integrated jitter with fractional spurs is 96fs_{rms} , while the fractional spurs remain below -61.2dBc . The measured performance of this work is summarized and compared with the prior arts (TABLE II). It achieves a FoM of -260.9dB with a 100MHz reference and smaller chip area.

IV. CONCLUSION

This work pushes fractional-N PLL's FoM down to -260.9dB with only a 100MHz reference by using power reduction and DTC delay reduction techniques and occupies only 0.11mm^2 core chip area by using a shared-PD-based

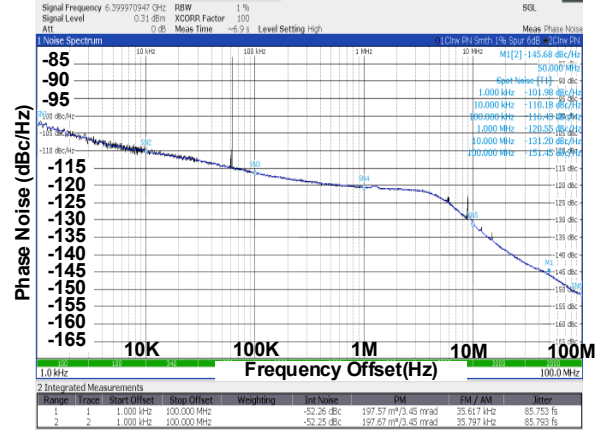


Fig. 6. Measured PLL's output phase noise spectrum in integer-N mode with $FCW=64$

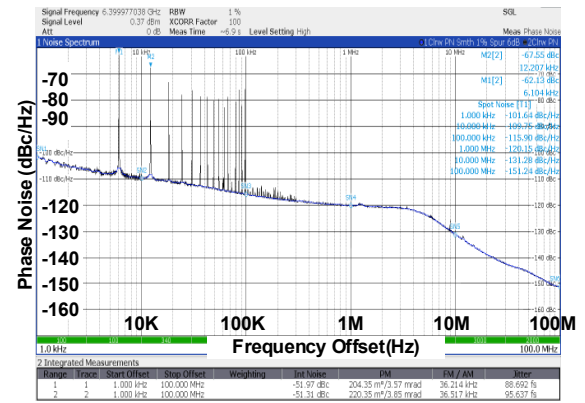


Fig. 7. Measured PLL's output phase noise spectrum in fractional-N mode with $FCW=64+2^{-14}$.

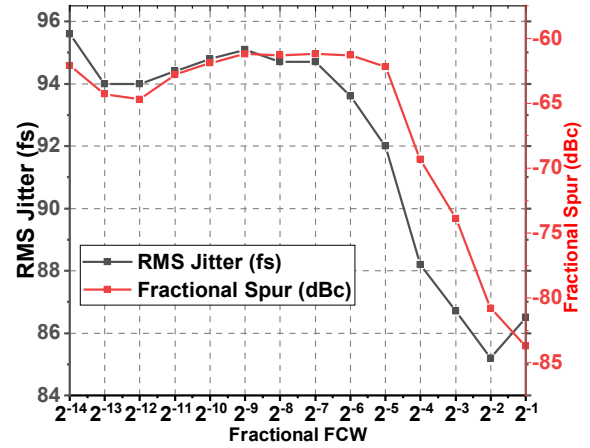


Fig. 8. Measured PLL's output rms jitter and fractional spur versus different fractional FCW with integer $FCW=64$.

hybrid loop without offset compensation. The gated-LMS calibration is extended to VCO DCC with DSM-1 to reduce DTC delay range to half of VCO period. CDAC-based DTC-SPD is used to avoid power and jitter contributed by fine DTC and also provide detection outputs for both analog proportional path and digital integral path.

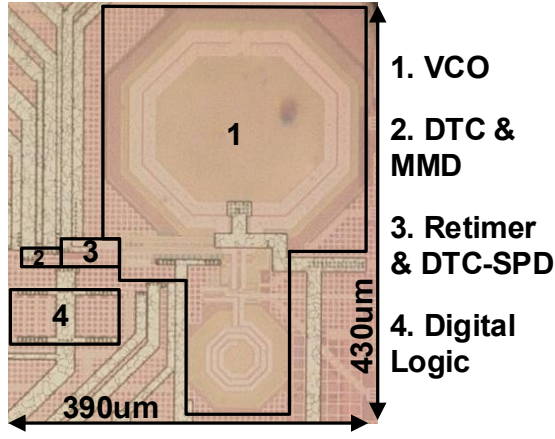


Fig. 9. Die photo of the presented fractional-N hybrid PLL

TABLE I. POWER CONSUMPTION AND CHIP AREA BREAKDOWN

Building Block	Power Consumption (mW)	Chip Area (mm ²)
VCO	0.53	0.0964
Retimer and DTC-SPD	0.15	0.0029
C-DTC	0.03	0.0016
MMD	0.07	
Digital Logic	0.1	0.0095
Total	0.88	0.1104

TABLE II. PERFORMANCE SUMMARY AND COMPARISON WITH PRIOR FRACTIONAL-N PLLS.

	This Work	JSS25 [1]	VLSI25 [3]	ISSCC25 [9]	ISSCC26 [10]
PLL Arch.	Hybrid	Analog	Analog	Analog	Analog
Ref. Freq. (MHz)	100	2285	100	80×2	250
Out. Freq. (GHz)	6.4 (6.2-8)	4.85 (4.8-5)	6.4 (6.1-7.9)	9.5 (7.3-9.5)	13.75 (13.1-14.5)
RMS Jitter(fs)	96	91	96.6	37.7	29.7
In-Band Frac. Spur (dBc)	-61.2	-64	-65	-64.8	-67.4
Reference Spur (dBc)	-72.6	-70	-71.7	-101	-73.2
Power (mW)	0.88	0.96	1.94	24.4	18.1
FoM*	-260.9	-261	-257.4	-254.6	-258
Area (mm ²)	0.11	0.18	0.23	0.39	0.34
Technology	28nm	7nm	40nm	22nm	28nm

* FoM=10×log₁₀[(Power/1mW)×(RMS Jitter/1s)²]

ACKNOWLEDGMENT

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